



# Artificial Neural Networks for Geodata

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# Our roadmap

Day 1:

- Into to Neural Nets
- Implementation (PyTorch)

Day 2:

- Autoencoders (AE), Variational AE and Generative Adversarial Nets
- Implementation (PyTorch)

Day 3:

- RNN, LSTM and Transformers
- Implementation (TensorFlow)

### Agenda

1) Background in Artificial Neural Networks (ANNs)

- Biological inspiration
- Applications: Classification, Regression
- Components of ANNs
- 2) Using libraries to build an ANN (PyTorch)
- Opmitizers
- Dropout
- Early stop
- Regularization
- Deeper nets

#### Evolution of ANNs



- 1) Biological Learning Theory (1943, 1949)
- 2) Perceptron (1958)
- 3) Backpropagation (1986)
- 4) Deep Learning (2006, 2007)

#### ANNs architecture



#### **Biological Neuron versus Artificial Neural Network**

Brain "inspired" model

- Not enough info about brain processing...
- But we know the basics:





Hubel and Wiesel, 1959-1968

Fukushima, 1980

#### Learning algorithms

"A computer program is said to learn from experience **E** with respect to some class of tasks **T** and performance measure **P**, if its performance at tasks in **T**, as measured by **P**, improves with experience **E**."

#### Tasks (T) Transcription Machine Translation Classification Anomaly detection Synthesis and sampling : Regression

#### Performance (P)

Accuracy rate

Adjusted R<sup>2</sup> RMSE/MSE/MAE

#### **Experience (E)**

Supervised Learning

Unsupervised Learning

**Reinforcement Learning** 



#### **Biological Neuron versus Artificial Neural Network**

Solves linear problems Can't solve the XOR problem







I2









Perceptron







sigmoid + polynomial transform







### Backpropagation

- Input x: Set the corresponding activation a<sup>1</sup> for the input layer.
- 2. Feedforward: For each l = 2, 3, ..., L compute  $z^{l} = w^{l}a^{l-1} + b^{l}$  and  $a^{l} = \sigma(z^{l})$ .
- 3. **Output error**  $\delta^L$ : Compute the vector  $\delta^L = \nabla_a C \odot \sigma'(z^L)$ .
- 4. Backpropagate the error: For each l = L 1, L 2, ..., 2compute  $\delta^l = ((w^{l+1})^T \delta^{l+1}) \odot \sigma'(z^l)$ .
- 5. **Output:** The gradient of the cost function is given by  $\frac{\partial C}{\partial w_{jk}^l} = a_k^{l-1} \delta_j^l \text{ and } \frac{\partial C}{\partial b_j^l} = \delta_j^l.$

$$\frac{\partial E}{\partial w_{ji}^{l}} = \frac{\partial E}{\partial a_{i}^{l}} \frac{\partial a_{i}^{l}}{\partial z_{j}^{l}} \frac{\partial (w_{ji}^{l} a_{i}^{l-1})}{\partial w_{ji}^{l}}$$



#### Gradient

$$\Delta w_k = -\frac{\partial E}{\partial w_k}$$
$$= -\frac{\partial}{\partial w_k} \left( \frac{1}{m} \sum_i (w^T X_i - y_i)_i^2 \right)$$

 $w_{i+1} = w_i + \Delta w_k$ 

Stochastic gradient descent (SGD)





Hyperparameters

• Learning rate ( $\alpha$ )

$$\Delta w_k = -\alpha \frac{\partial E}{\partial w_k}$$
$$= -\alpha \frac{\partial}{\partial w_k} \left( \frac{1}{m} \sum_i (w^T X_i - y_i)_i^2 \right)$$

 $w_{i+1} = w_i + \Delta w_k$ 

Stochastic gradient descent (SGD)

Practical test: lr\_val = [1; 0.1; 0.01] momentum\_val = 0 nesterov\_val = 'False' decay\_val = 1e-6



Result of a large learning rate  $\alpha$ 

#### Hyperparameters

• Learning rate ( $\alpha$ )

$$\Delta w_k = -\alpha \frac{\partial E}{\partial w_k}$$
$$= -\alpha \frac{\partial}{\partial w_k} \left( \frac{1}{m} \sum_i (w^T X_i - y_i)_i^2 \right)^2$$

 $w_{i+1} = w_i + \Delta w_k$ 

Stochastic gradient descent (SGD)



Hyperparameters

• Learning rate ( $\alpha$ )

 $\Delta w_k = -\alpha \frac{\partial E}{\partial w_k}$  $= -\alpha \frac{\partial}{\partial w_k} \left( \frac{1}{m} \sum_i (w^T X_i - y_i)_i^2 \right)$ 

 $w_{i+1} = w_i + \Delta w_k$ 

Stochastic gradient descent (SGD)



Multiple samples

Hyperparameters

- Learning rate ( $\alpha$ )
- Momentum ( $\beta$ )

$$v_{i+1} = v\beta - \alpha \frac{\partial}{\partial w_k} \left( \frac{1}{m} \sum_i (w^T X_i - y_i)_i^2 \right)$$
$$w_{i+1} = w_i + v$$



#### Stochastic gradient descent with momentum (SGD+Momentum)

Hard to pick right hyperparameters

- Small learning rate: long convergence time
- Large learning rate: convergence problems

#### Adagrad: adapts learning rate to each parameter

$$\Delta w_{k,t} = -\alpha \frac{\partial E_t}{\partial w_{k,t}} = -\alpha \nabla_w E(w_t)$$

$$g_{t,i} = \nabla_w E(w_{t,i})$$

$$G_{t+1,i} = G_{t,i} + g_{t,i} \odot g_{t,i}$$

$$w_{t+1,i} = w_{t,i} - \frac{\alpha}{\sqrt{G_{t,i} + \epsilon}} g_{t,i}$$

RMSprop: decaying average of the past squared gradients

Adadelta

$$E[g^2]_t = \gamma E[g^2]_{t-1} + (1 - \gamma)g_t^2$$
  
Decaying average

$$E[\Delta_w^2]_t = \gamma E[\Delta_w^2]_{t-1} + (1-\gamma)\Delta_w^2$$
$$\Delta w_t = \frac{\sqrt{E[\Delta_w^2]_t + \epsilon}}{\sqrt{G_{t,i} + \epsilon}} g_t$$

$$\Delta w_{k,t} = -\alpha \frac{\partial E_t}{\partial w_{k,t}} = -\alpha \nabla_w E(w_t) = -\alpha g_{t,i}$$

 $g_{t,i} = \nabla_{w} E(w_{t,i})$   $G_{t+1,i} = \gamma G_{t,i} + (1-\gamma)g_{t,i} \odot g_{t,i}$  $w_{t+1,i} = w_{t,i} - \frac{\alpha}{\sqrt{G_{t,i} + \epsilon}}g_{t,i}$ 

#### ADAM: decaying average of the past squared gradients and momentum

RMSprop / Adadelta

$$g_{t,i} = \nabla_{w} E(w_{t,i})$$

$$G_{t+1,i} = \gamma G_{t,i} + (1-\gamma)g_{t,i} \odot g_{t,i}$$

$$v_{t} = \beta_{2}v_{t-1} + (1-\beta_{2})g_{t}^{2}$$

$$m_{t} = \beta_{1}m_{t-1} + (1-\beta_{1})g_{t}$$

$$\widehat{m}_{t} = \frac{m_{t}}{1-\beta_{1}^{t}}$$

$$w_{t+1,i} = w_{t,i} - \frac{\alpha}{\sqrt{\hat{v}_t} + \epsilon} \hat{m}_t$$



Which optimizer is the best?

### Regularization

Dropout: accuracy in the absence of certain information

• Prevent dependence on any one (or any small combination) of neurons



### Capacity, Overfitting and Underfitting

1) Make training error small

2) Make the gap between training and test error small



#### How training works

- 1. In each *epoch*, randomly shuffle the training data
- 2. Partition the shuffled training data into *mini-batches*
- For each mini-batch, apply a single step of gradient descent
  - Gradients are calculated via *backpropagation* (the next topic)
- 4. Train for multiple epochs

# Debugging a neural network

- What can we do?
  - Should we change the learning rate?
  - Should we initialize differently?
  - Do we need more training data?
  - Should we change the architecture?
  - Should we run for more epochs?
  - Are the features relevant for the problem (i.e. is the Bayes error rate reasonable)?
- Debugging is an art
  - We'll develop good heuristics for choosing good architectures and hyper parameters